

# **MATERIALS SCIENCE**

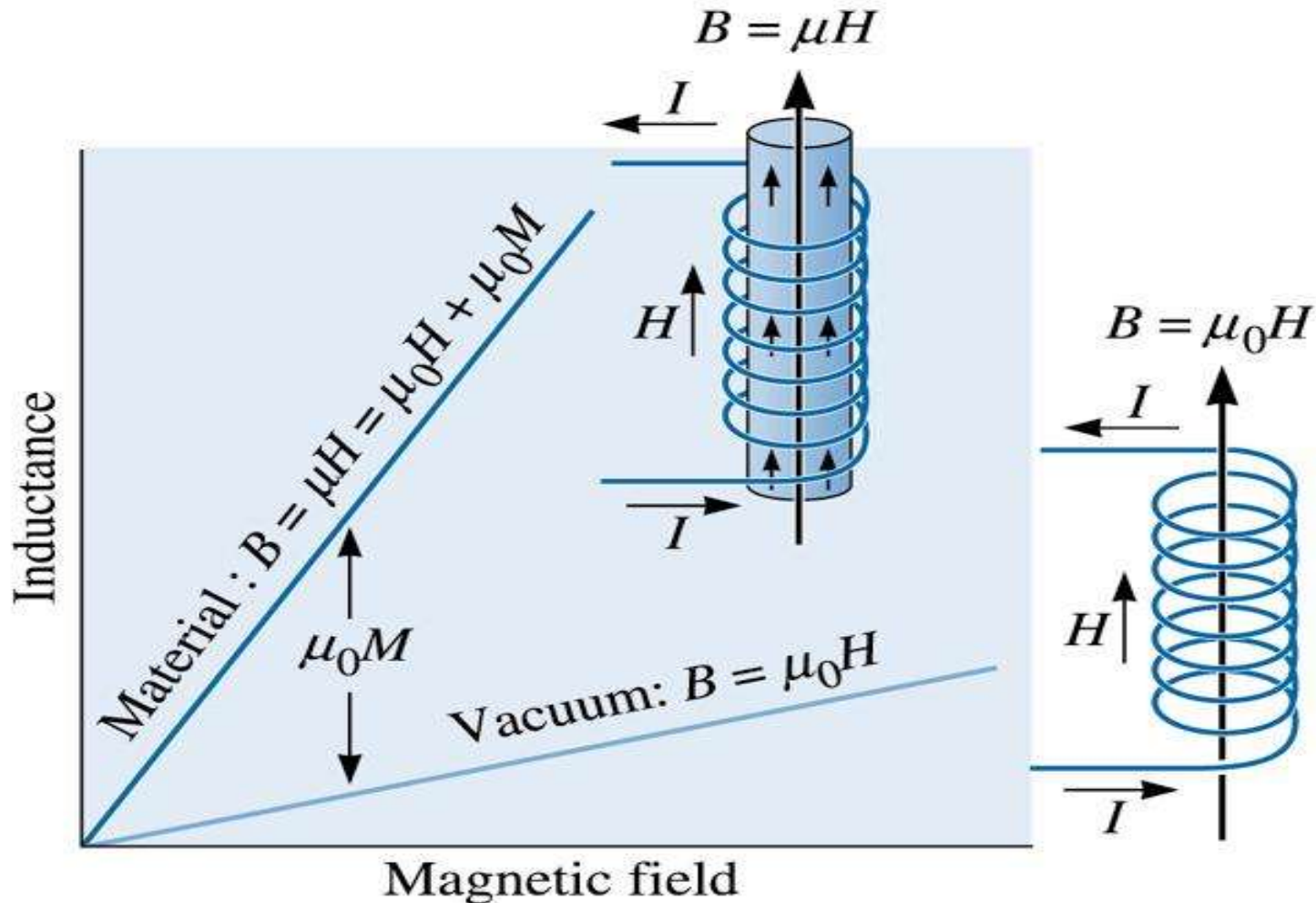
## **SSP 2412**

### **MAGNETIC & OPTICAL PROPERTIES**

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# Main Topics

- Introduction to Magnetic Properties
- Magnetism on the Microscopic Scale.
- Diamagnetism.
- Paramagnetism.
- Ferromagnetism.
- Applications



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**A current passing through a coil sets up a magnetic field  $H$  with a flux density  $B$ . The flux density is higher when a magnetic core is placed within the coil.**

## EXAMPLE & SOLUTION

The magnetic field  $H$  produced by the coil.

$$H = \frac{nI}{l} = \frac{(10)(0.01 \text{ A})}{0.01 \text{ m}} = 10 \text{ A/m}$$

$$H = (10 \text{ A/m})(4\pi \times 10^{-3} \text{ oersted/A/m}) = 0.126 \text{ oersted}$$

The permeability of the core material must be:

$$\mu = \frac{B}{H} = \frac{2000}{0.126} = 15,873 \text{ gauss/oersted}$$

The relative permeability of the core material must be at least:

$$\mu_r = \frac{\mu}{\mu_0} = \frac{15,873}{1} = 15,873$$

# Macroscopic description of magnetism

magnetic induction

in vacuum

magnetic field

$$\mathbf{B} = \mu_0 \mathbf{H}$$

$$\mu_0 = 4\pi 10^{-7} \text{Vs/Am} = 4\pi 10^{-7} \text{T}^2 \text{m}^3 \text{J}^{-1}$$

in matter

magnetization

$$\mathbf{B} = \mu_0 (\mathbf{H} + \mathbf{M}) = \mathbf{B}_0 + \mu_0 \mathbf{M}$$

we interpret  $\mathbf{B}_0$  as the “external field”

magnetic

susceptibility

$$\mu_0 \mathbf{M} = \chi \mathbf{B}_0$$

$$\mathbf{M} = \frac{N}{V} \mu$$

magnetic dipole

moment

potential energy of one dipole in the external field:

$$U = -\mu \mathbf{B}_0$$

## Units

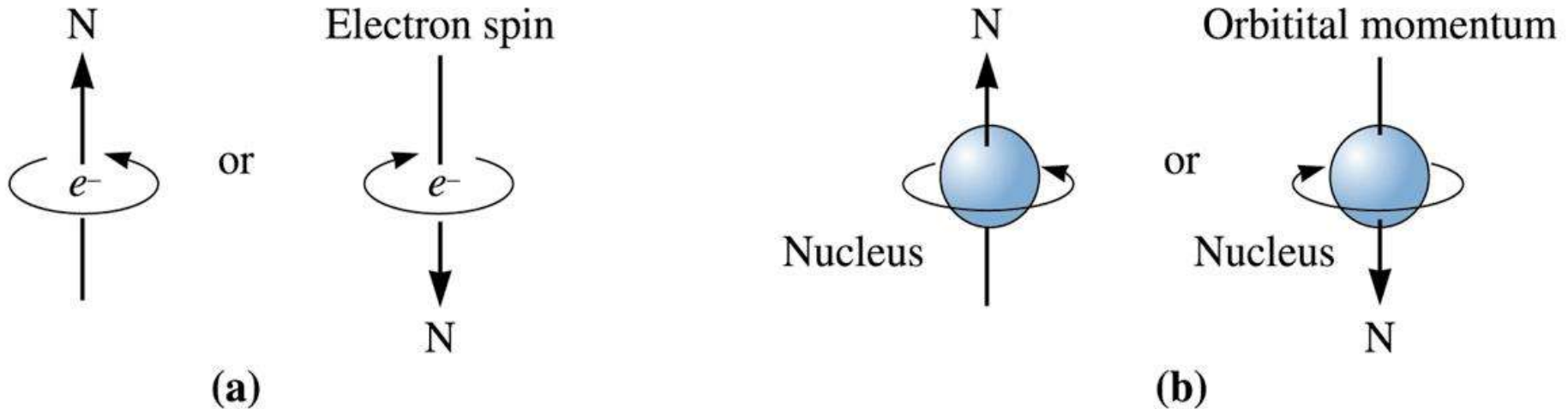
$$\begin{array}{ccccccc}
 \text{T} & & \text{T}^2 \text{m}^3 \text{J}^{-1} & & \text{T} & & \text{T}^{-1} \text{m}^{-3} \text{J} \\
 \downarrow & & \downarrow & & \downarrow & & \swarrow \\
 \mathbf{B} & = & \mu_0 (\mathbf{H} + \mathbf{M}) & = & \mathbf{B}_0 & + & \mu_0 \mathbf{M}
 \end{array}$$

- Both,  $\mathbf{B}$  and  $\mathbf{B}_0$  are measured in Tesla (T)
- 1 T is a strong field. The magnetic field for the earth is only in the order of  $10^{-5}$  T.

# Magnetism on Microscopic Scale

- Electrons can generate magnetism in three ways: i) As moving charges as current, ii) Due to their **spin** and iii) Due to their **orbital** rotation around a core.
- The later two mechanisms (**spin, orbital**) are responsible for magnetic behavior in matter.
- **Bohr magneton** (symbol  $\mu_B$ ) is a physical constant and the natural unit for expressing an electron magnetic dipole moment (Magnetic moment of an electron)

# Spin & Orbit



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**Origin of magnetic dipoles: (a) The spin of the electron produces a magnetic field with a direction dependent on the quantum number  $m_s$ . (b) Electrons orbiting around the nucleus create a magnetic field around the atom.**



# Spins in 3d Metals

**TABLE 19-1** ■ *The electron spins in the 3d energy level in transition metals, with arrows indicating the direction of spin*

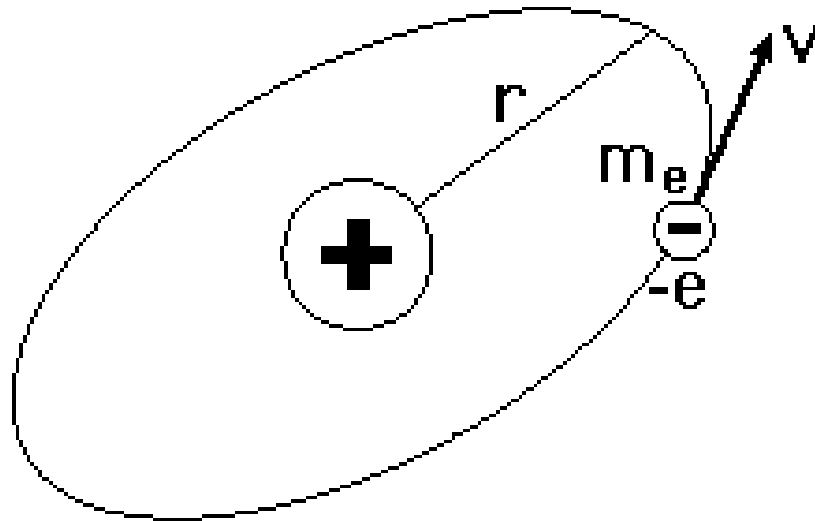
Metal	3d					4s
Sc	↑					↑↓
Ti	↑	↑				↑↓
V	↑	↑	↑			↑↓
Cr	↑	↑	↑	↑	↑	↑
Mn	↑	↑	↑	↑	↑	↑↓
Fe	↑↓	↑	↑	↑	↑	↑↓
Co	↑↓	↑↓	↑	↑	↑	↑↓
Ni	↑↓	↑↓	↑↓	↑	↑	↑↓
Cu	↑↓	↑↓	↑↓	↑↓	↑↓	↑

# Ferromagnetic elements

H																	He	
Li	Be											B	C	N	O	F	Ne	
Na	Mg											Al	Si	P	S	Cl	Ar	
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr	
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe	
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn	
Fr	Ra	Ac	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Uub							
			Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu		
			Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr		

and many alloys are also ferromagnetic

# Electron Orbit Magnetic Moment



Effective current is

$$I = \frac{-e}{T} = \frac{ev}{2\pi r} \quad \text{or} \quad I = \frac{-em_e v r}{2\pi m_e r^2}$$

$T$  = period of orbit

$L$  = orbital **angular momentum**

Magnetic moment,

$$\mu = IA = \frac{-e}{2m_e} L$$

The magnetic moment associated with an electron orbit is given by

$$\mu = IA = \frac{-e}{2m_e} L$$

Taking into account the quantization of angular momentum for such orbits, the magnitude of the magnetic moment can be written

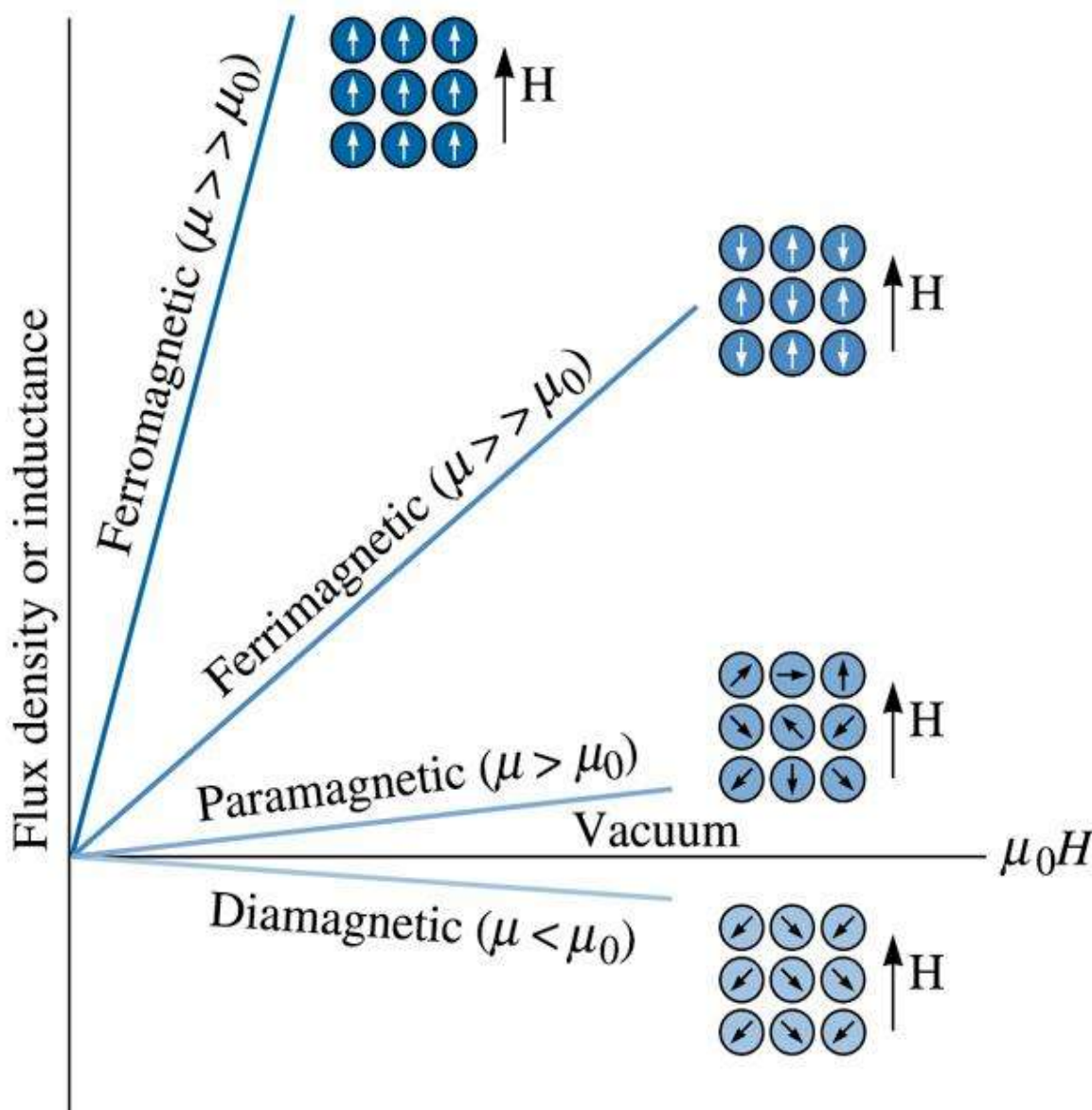
$$\mu = \frac{-e}{2m_e} L = \frac{-e}{2m_e} \sqrt{l(l+1)} \hbar = \sqrt{l(l+1)} \mu_B$$

A unit of magnetic moment called the **Bohr magneton** is,

$$\mu_B = \frac{e \hbar}{2m_e} = 9.27 \times 10^{-24} \text{ J/T} = 5.79 \times 10^{-5} \text{ eV/T}$$

# Magnetic Properties

- There are **three** types of magnetic behavior. The external field in materials can be
  - **weakened** ( $\chi_m < 0$  or  $K_m < 1$ ) this is called **diamagnetism**
  - **slightly intensified**, ( $\chi_m > 0$  or  $K_m > 1$ ) this is called **paramagnetism**
  - **considerably intensified**, ( $\chi_m \gg 0$  or  $K_m \gg 1$ ) called **ferromagnetism**.



The effect of the core material on the flux density. The magnetic moment opposes the field in diamagnetic materials. Progressively stronger moments are present in paramagnetic, ferrimagnetic, and ferromagnetic materials for the same applied field.

# DIAMAGNETISM

Diamagnetism: negative susceptibility, the magnetization opposes the external field, the potential energy is lowered when moving the magnetized bodies to a lower field strength. A diamagnet opposes both poles of a magnet. Diamagnetism is caused by “currents” induced by the external field. According to Lenz’ law, these currents always lead to a field opposing the external field.

# Diamagnetism

- Due to an external magnetic field a radial force acts on the electron. It points toward or out of the center depending on the direction of the field. The force can't change the radius but if it points toward the center it speeds the electron and if out it slows it. This leads to a change in the magnetic moment which is always opposite to the field. So the field is weakened.



# PARAMAGNETISM

Paramagnetism occurs in materials whose atoms have permanent magnetic dipole moments; it makes no difference whether these dipole moments are of the orbital or spin types.

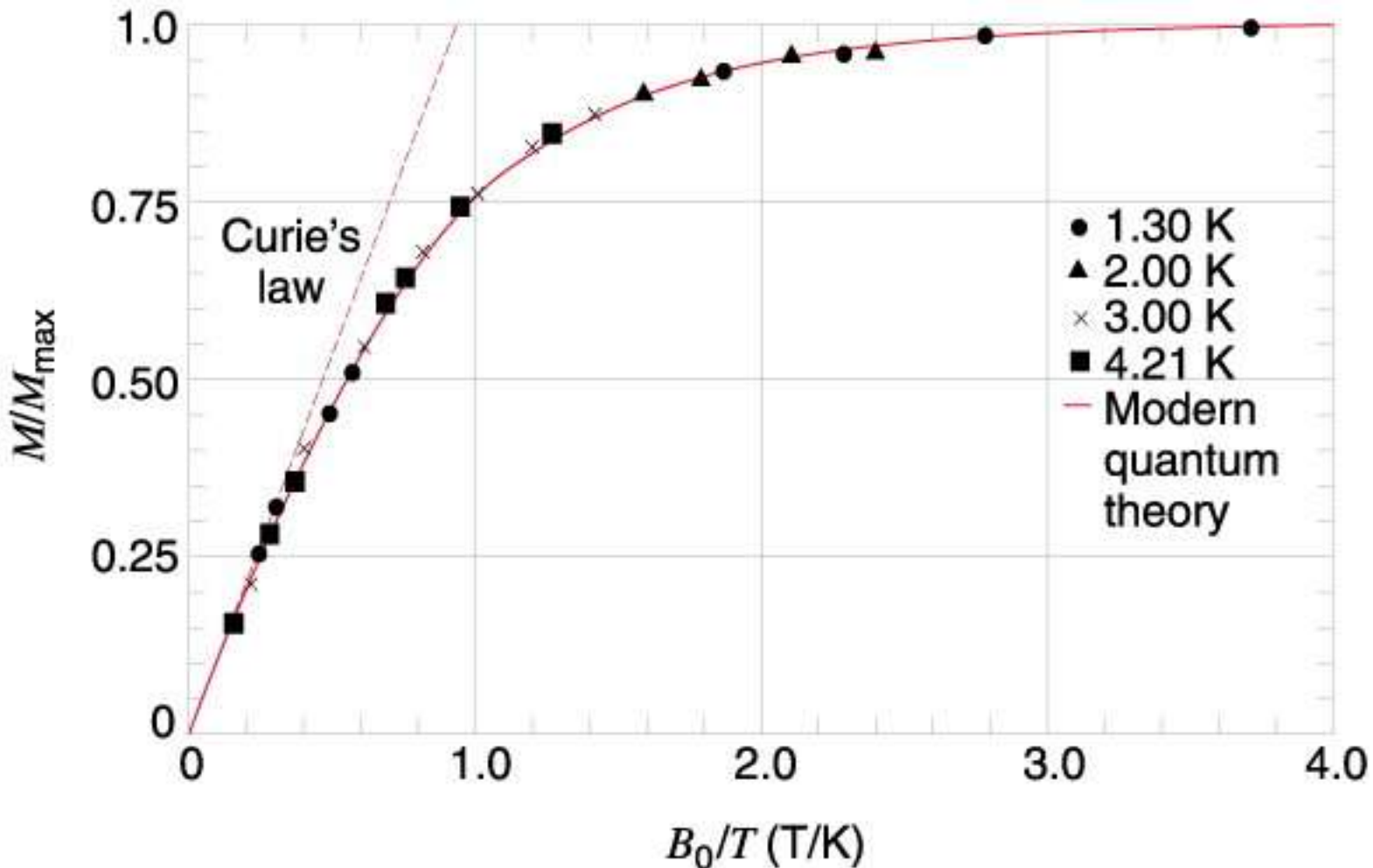
The paramagnetic materials at room temperature are Chromium, Tungsten, Aluminium, and Magnesium.

# Paramagnetism

$$M = \frac{\text{measured magnetic moment}}{\text{volume}}$$

$$M = C \frac{B_0}{T}$$

The thermal motion of the atoms tends to disturb the alignment of the dipoles, and consequently the magnetization (M) decreases with increasing temperature following Curie's law



Paramagnetism: Figure shows the ratio  $M/M_{max}$  as a function of  $B_{ext}/T$ . It is a magnetization curve.

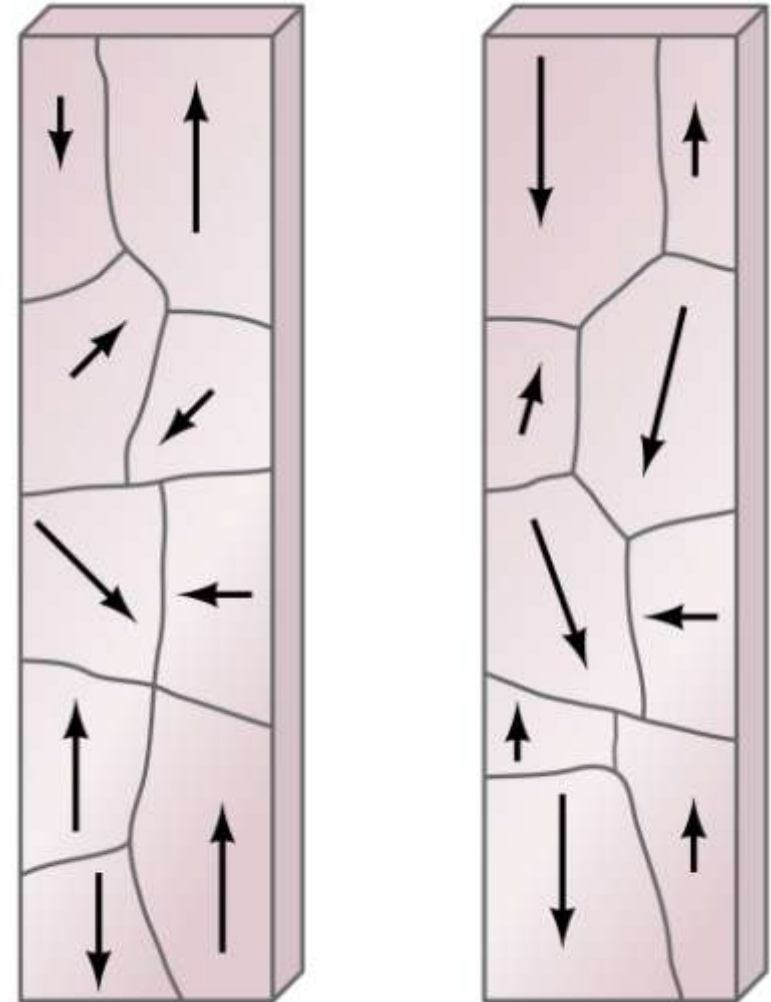
# FERROMAGNETISM

Ferromagnetic materials are those that can become strongly magnetized, with all spins in parallel, such as Fe, Co, Gd and Ni. These materials are made up of tiny regions called domains; the magnetic field in each domain is in a single direction.

Changes in spin directions (antiferromagnetic) and reduction spin magnitude (ferrimagnetic) cause deviation from original ferromagnetic.

# Domains and Hysteresis in Ferromagnetism:

When the material is unmagnetized, the domains are randomly oriented. They can be partially or fully aligned by placing the material in an external magnetic field.



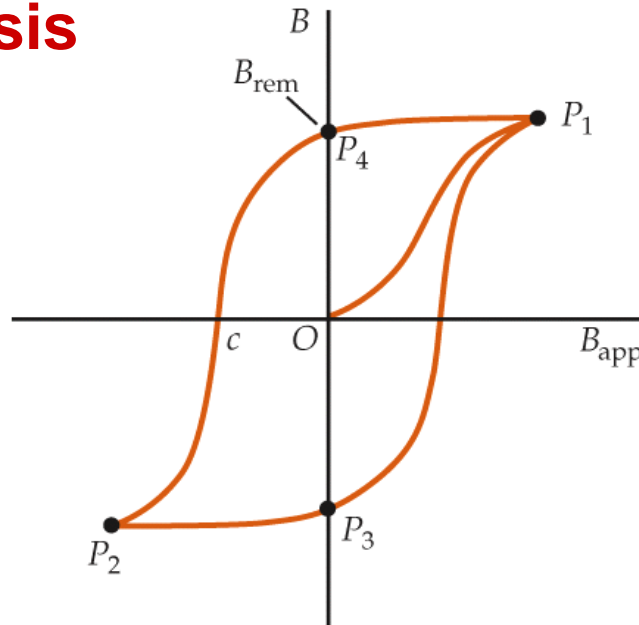
(a)

(b)

# Ferromagnetism

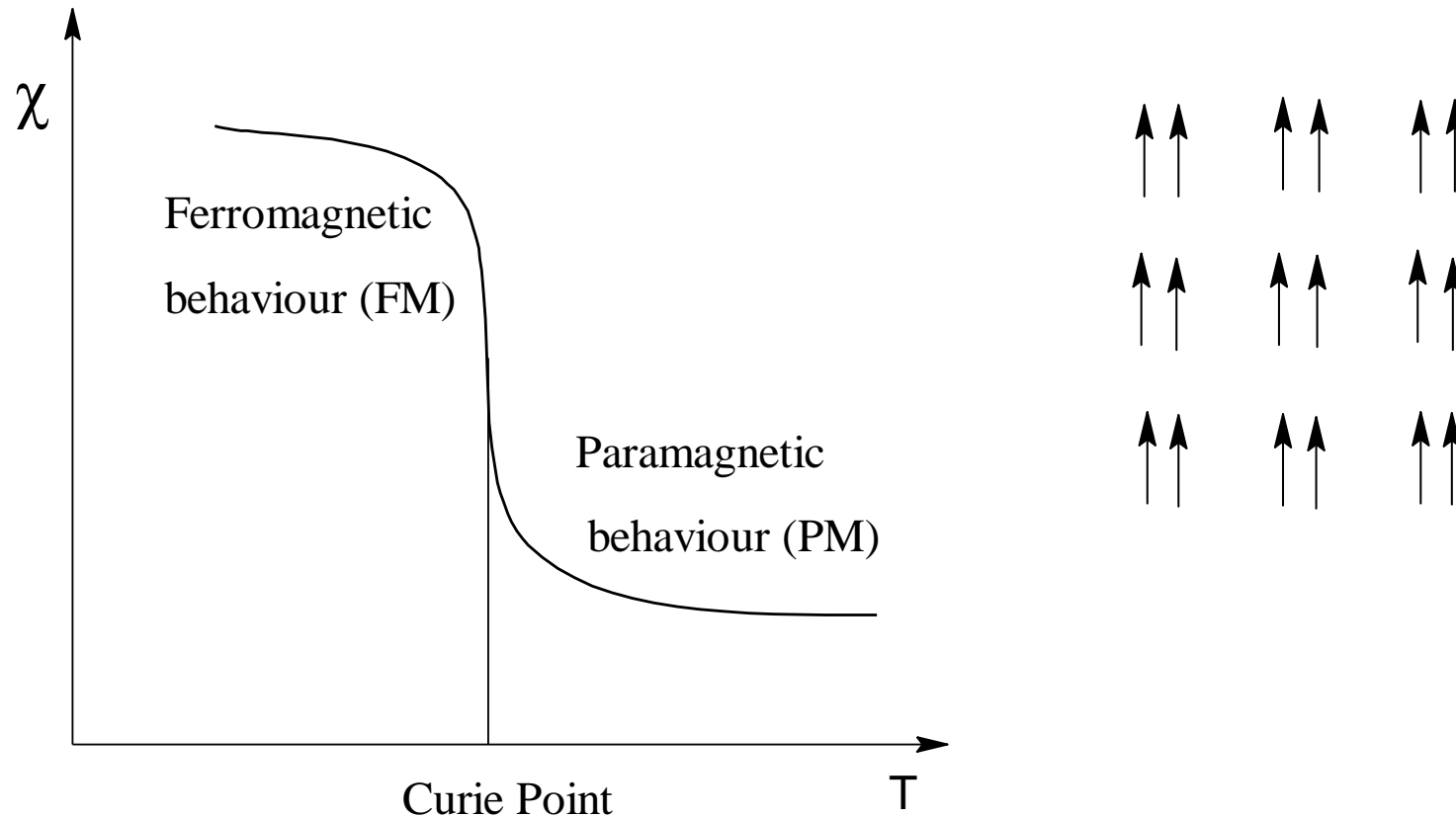
In ferromagnets, some magnetization will remain after the applied field is reduced to zero, yielding **permanent magnets**. Such materials exhibit **hysteresis**

Starting with unmagnetized material and no magnetic field, the magnetic field can be increased, decreased, reversed, and the cycle repeated. The resulting plot of the total magnetic field within the ferromagnet is called a hysteresis curve.



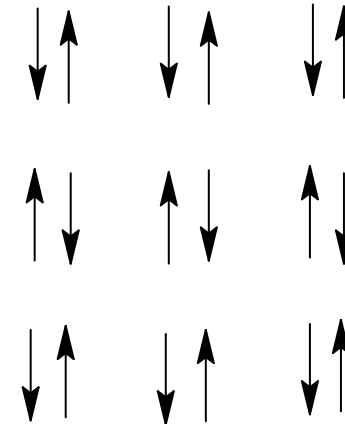
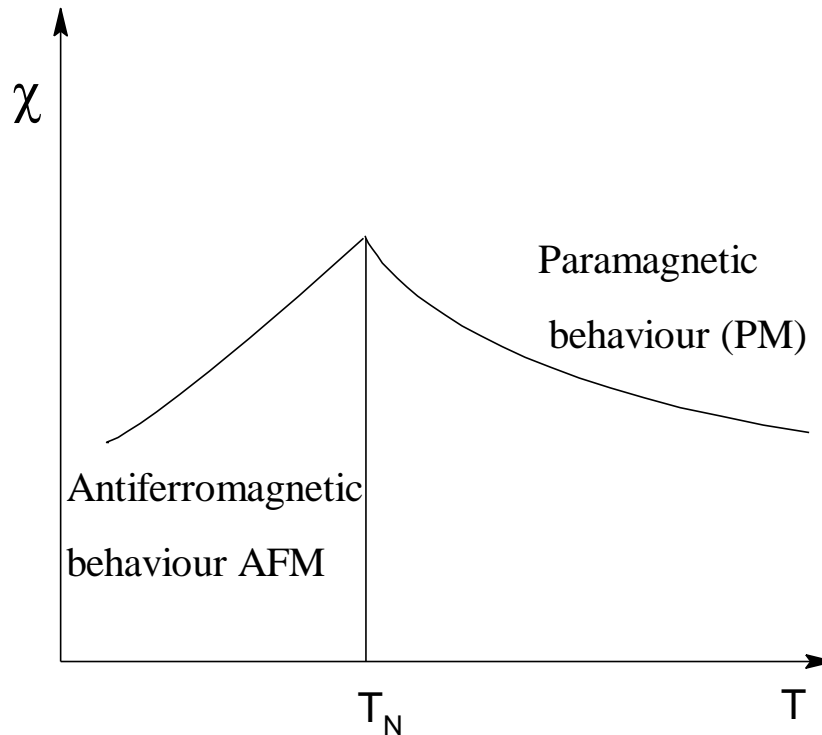
# Ferromagnetism

$\chi_m$  positive with spins parallel below  $T_c$



# Antiferromagnetism

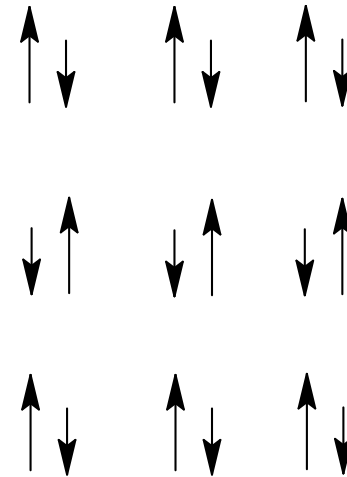
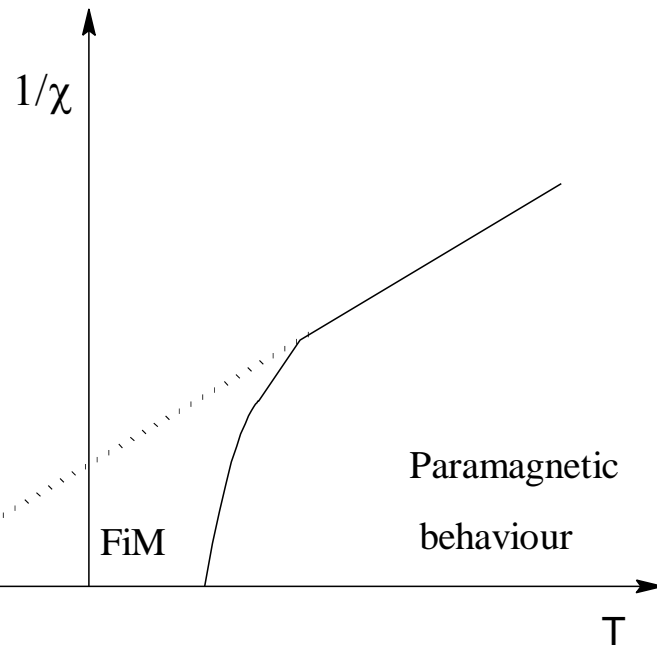
- $\chi_m$  negative with spins antiparallel below  $T_N$





# Ferrimagnetism

- $\chi_m$  negative with spins of unequal magnitude antiparallel below critical T



# COMPARISON OF MAGNETIC PROPERTIES

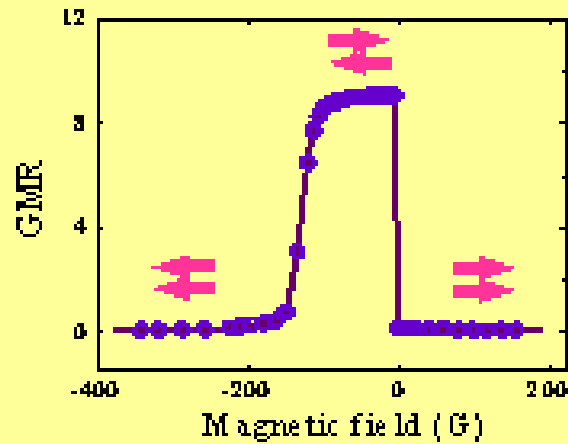
TYPE	SUSCEPTIBILITY $\chi_m$	TEMPERATURE DEPENDENT, $T$	EXAMPLES
Diamagnet	a) small & negative b) medium & negative c) large & negative	a) $\chi_m \propto T$ b) $\chi_m \propto T$ and $H$ c) Exist below critical temp. $T_c$	Organic materials, light elements and alkali metals
Paramagnet	a) small & positive b) large & positive	a) $\chi_m$ not $\propto T$ b) $\chi_m \propto 1/T$	Alkali metals, transition metals, rare earth metals
Ferromagnet	Very large and positive	$T > 0$ , $\chi_m = 1/(T - \theta)$ $T < 0$ , $\chi_m$ is complex	Transition metals and rare earth metals
Antiferromagnet	Small and positive	$T > T_N$ , $\chi_m = 1/(T + \theta)$ $T < T_N$ , $\chi_m \propto T$	Salts and transition metals
Ferrimagnet	Very large and positive	$T > T_N$ , $\chi_m \propto 1/(T \pm \theta)$ $T < T_N$ , $\chi_m$ complex	Ferrites, ferrous

$T_N$  : Neel temperature;  $\theta$  : Curie temperature

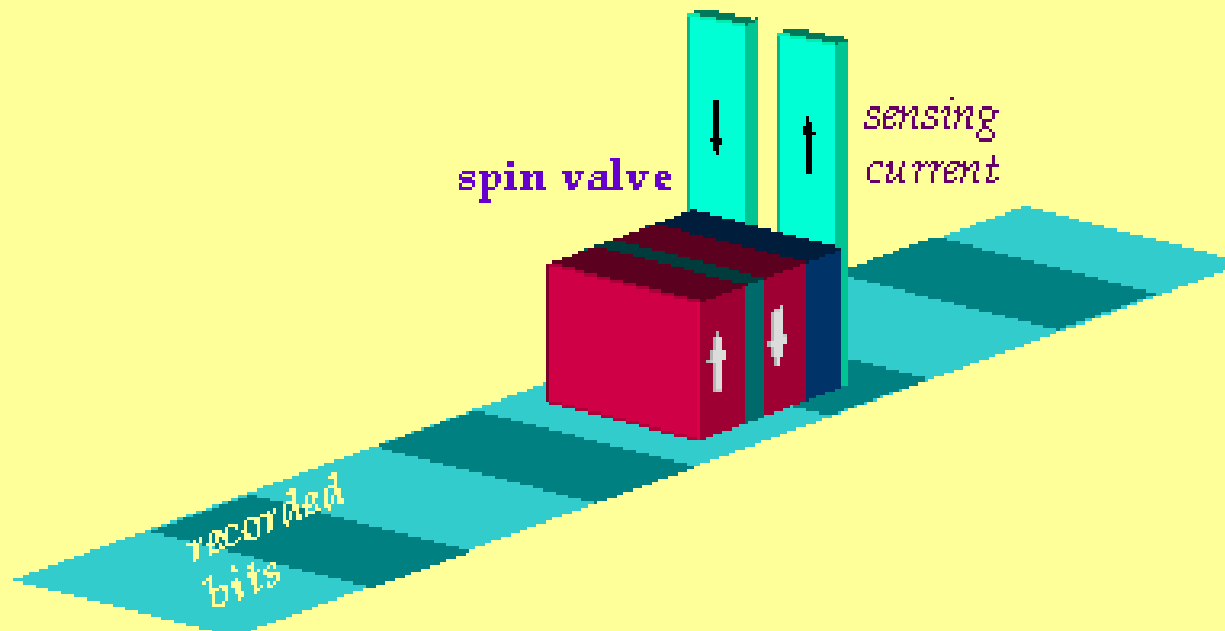
# Applications of Magnetic Materials

- **Soft Magnetic Materials** - Ferromagnetic materials are often used to enhance the magnetic flux density ( $B$ ) produced when an electric current is passed through the material. Applications include cores for electromagnets, electric motors, transformers, generators, and other electrical equipment.
- **Data Storage Materials** - Magnetic materials are used for data storage.
- **Permanent Magnets** - Magnetic materials are used to make strong permanent magnets
- **Power** - The strength of a permanent magnet as expressed by the maximum product of the inductance and magnetic field.
- **Sensor** – Based on giant magnetoresistance (GMR)

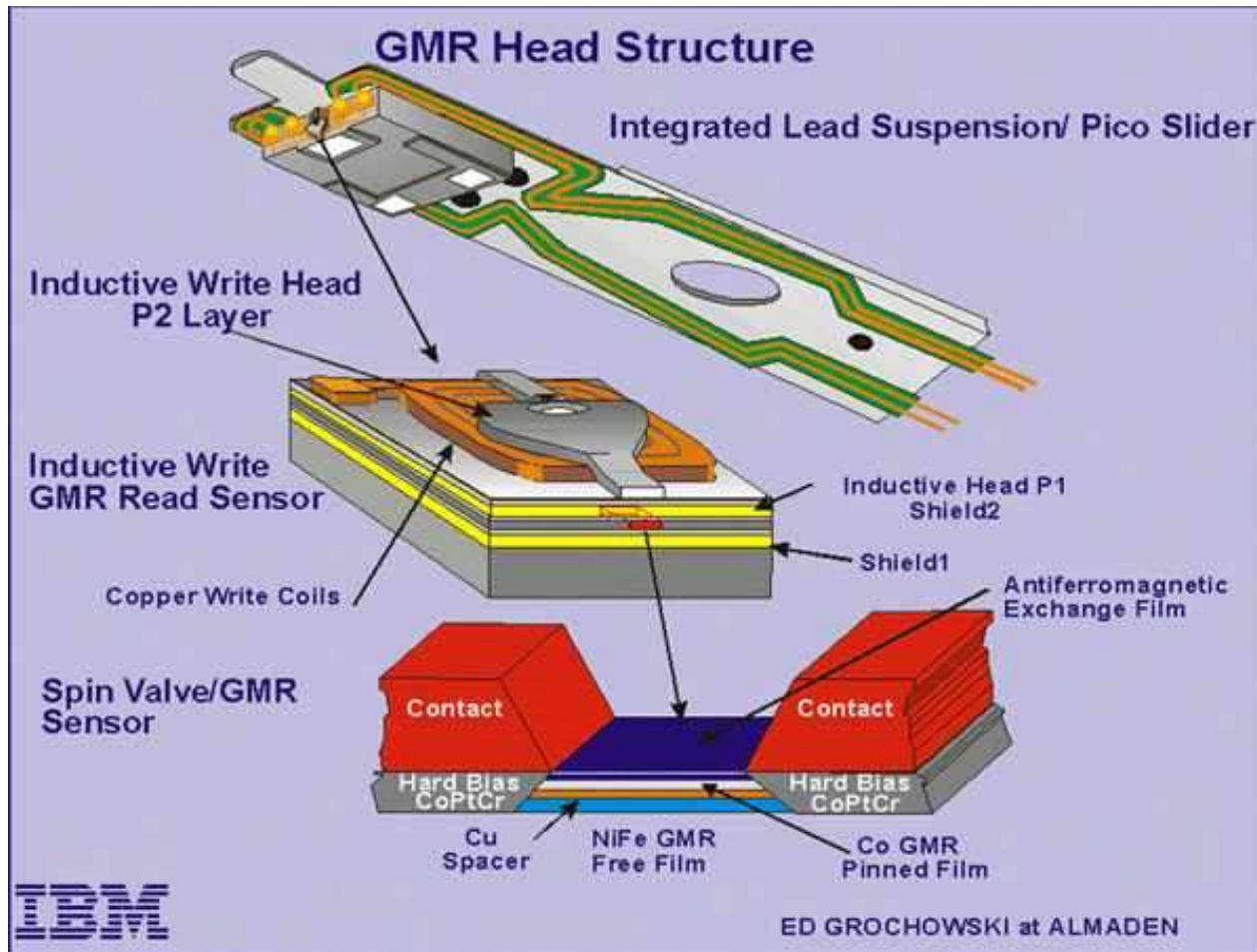
# Magnetic field sensor



Spin valve



# GMR Head



# SUMMARY

- A magnetic field can be produced by:
  - putting a current through a coil.
- **Magnetic induction:**
  - occurs when a material is subjected to a magnetic field.
  - is a change in magnetic moment from electrons.
- Types of material response to a field are:
  - ferro-** or **ferri-magnetic** (large magnetic induction)
  - paramagnetic** (poor magnetic induction)
  - diamagnetic** (opposing magnetic moment)
- **Hard magnets:** large **coercivity**.
- **Soft magnets:** small coercivity.
- Applications: :
  - Magnetic storage media
  - GMR sensor

# Optical Properties of Materials

## Optical Properties of Materials

Interaction of electromagnetic radiation (light) with a material

- Absorption
- Reflection
- Transmission

Absorptivity

Reflectivity

Transmissivity

Total Intensity / Initial Intensity  $I_0$

$$1 = I_A/I_0 + I_R/I_0 + I_T/I_0$$

$$I_0 = I_A + I_R + I_T$$

$$1 = A + R + T$$

A material cannot simultaneously be highly absorptive, reflective and transmissive



# Optical coefficients

propagation through  
the medium

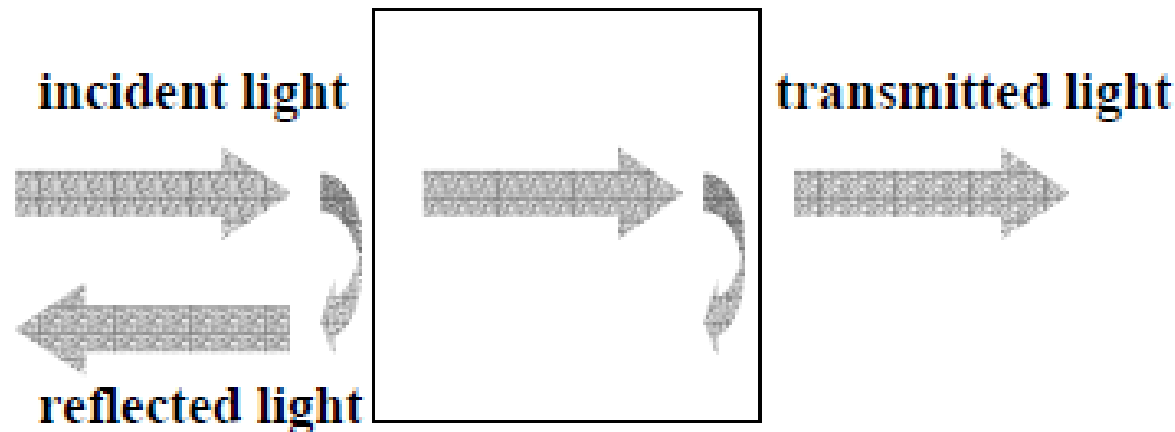
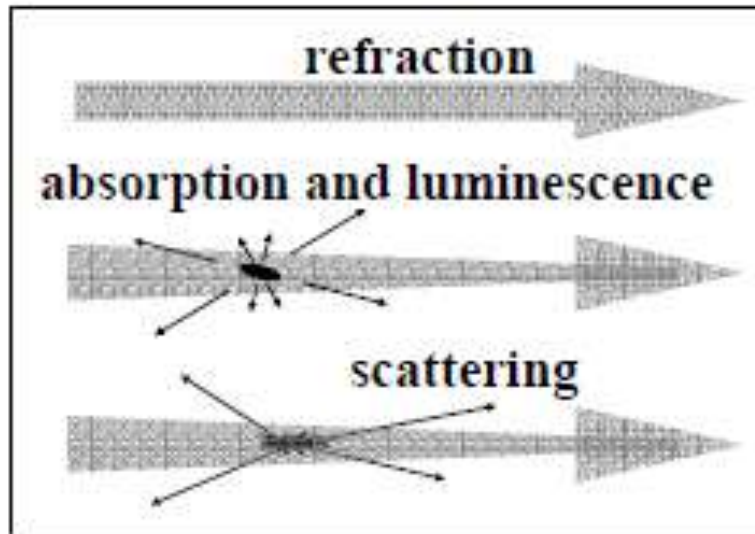


Figure 1.1: Optical coefficients

- Reflectivity = reflected / incident power
- Transmissivity = transmitted / incident power
- $T + R = 1$  if medium is transparent

# Propagation



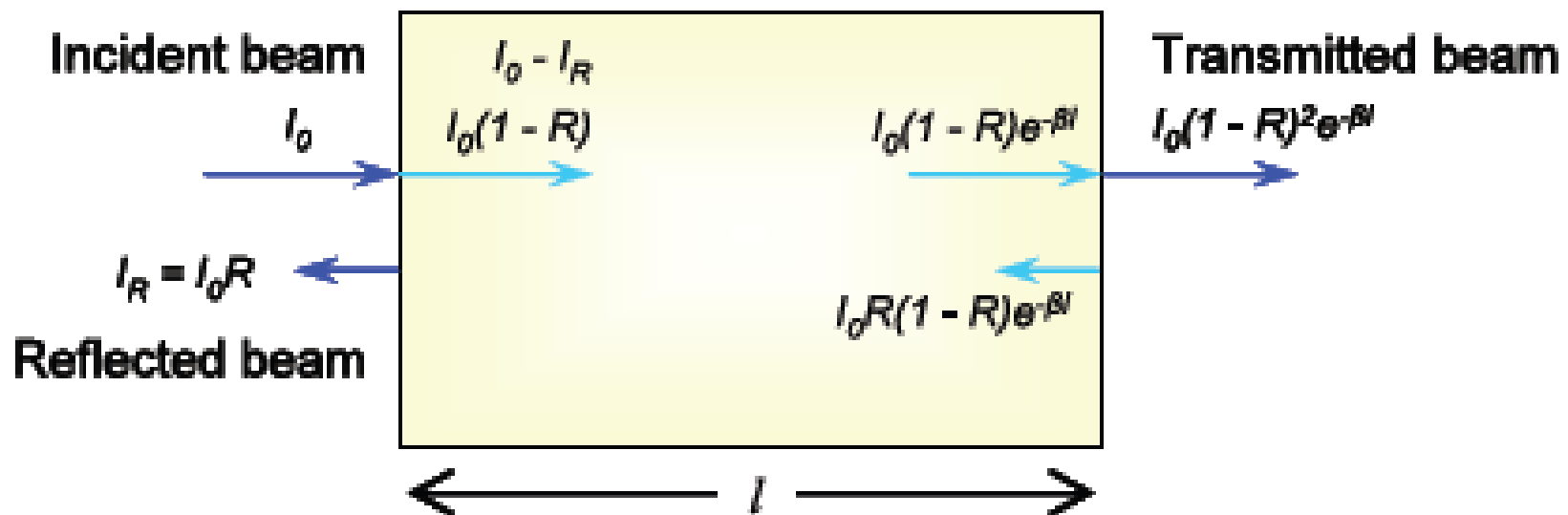
**Figure 1.2:**  
**Propagation of**  
**light through a**  
**medium**

- Velocity  $v = c/n$ ,  $n$  is the refractive index
- $I(z) = I_0 \exp(-\alpha z)$ ,  $\alpha$  is the absorption coefficient
- $T = (1-R_1) \exp(-\alpha L) (1-R_2)$
- **Luminescence** : re-emission at lower frequency
- **scattering**: *elastic*- change of direction  
*inelastic* - change of direction and frequency

# Optical Properties of Metals and Alloys

Shininess and inability to transmit visible light indicates

- high absorption    linear absorption coefficient  $\beta$
- high reflection    (up to  $R = 1$ )



$\beta$  and  $R$  determine how light interacts with a material

# Reflectance and color - Electronic effects

Empty electronic states above occupied levels

Light absorption:



Au

- e<sup>-</sup> promotion

- decay

Ag

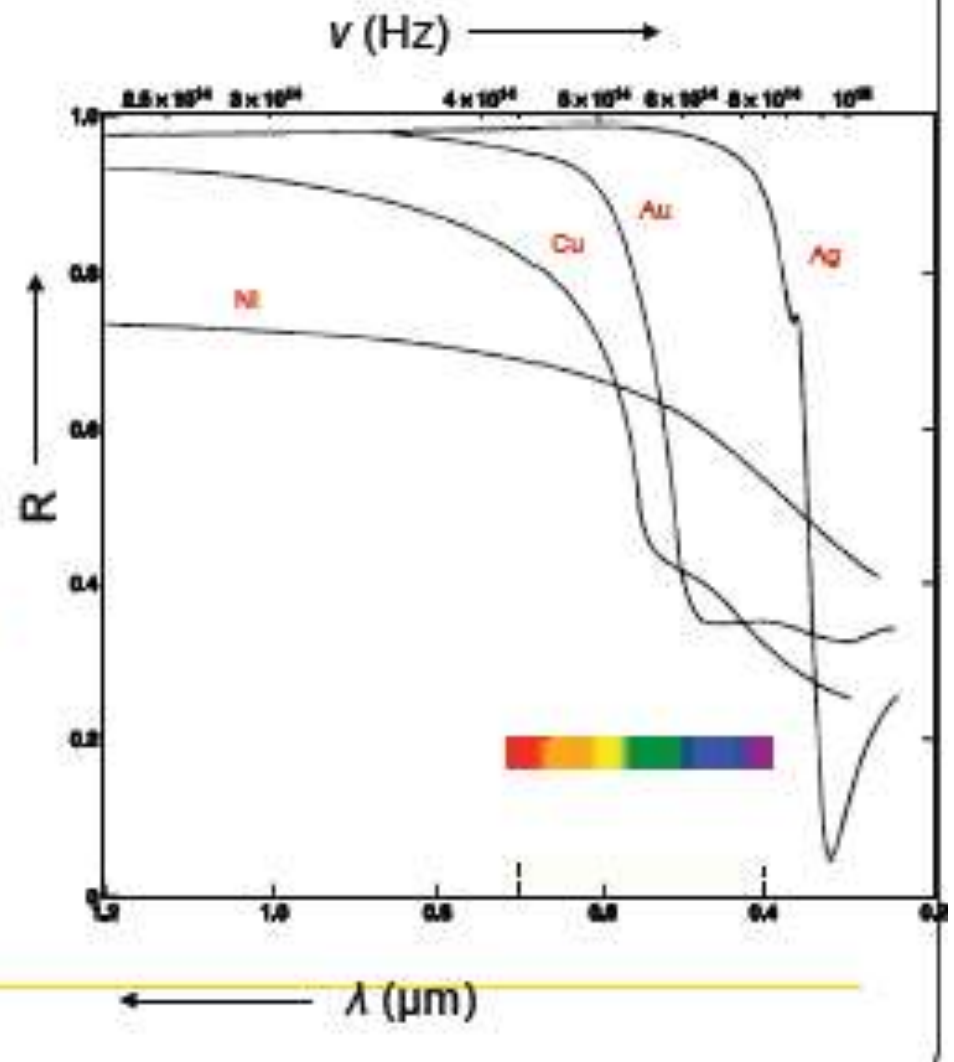
- reemission

- reflectivity

Cu

- dependent on  
frequency

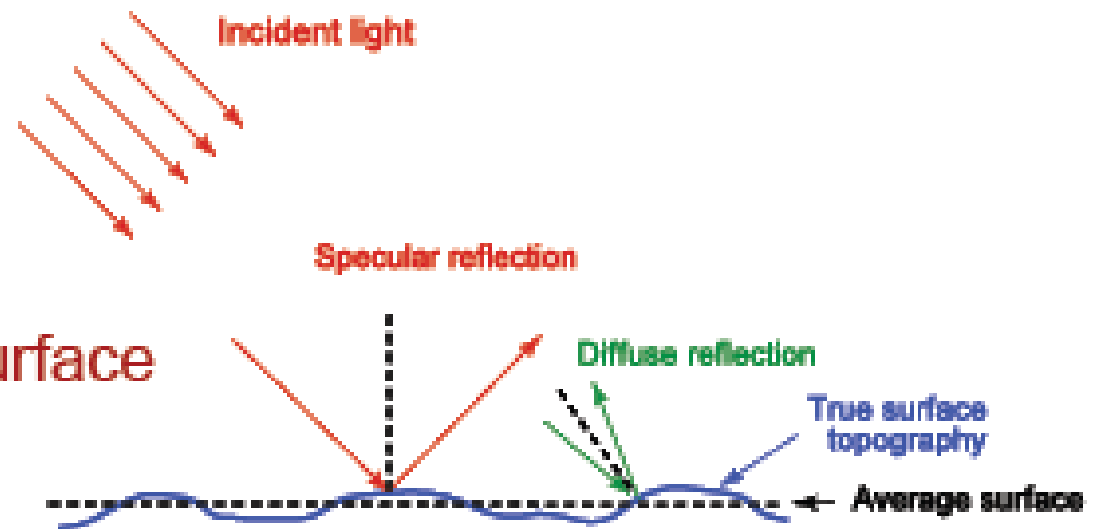
Ni



# Reflectance and color - Surface texture

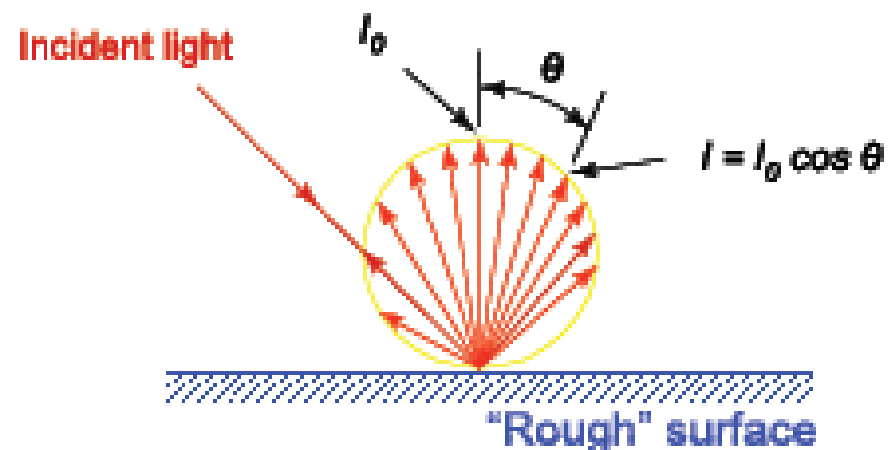
## Specular reflection

- smooth or mirror-like surface

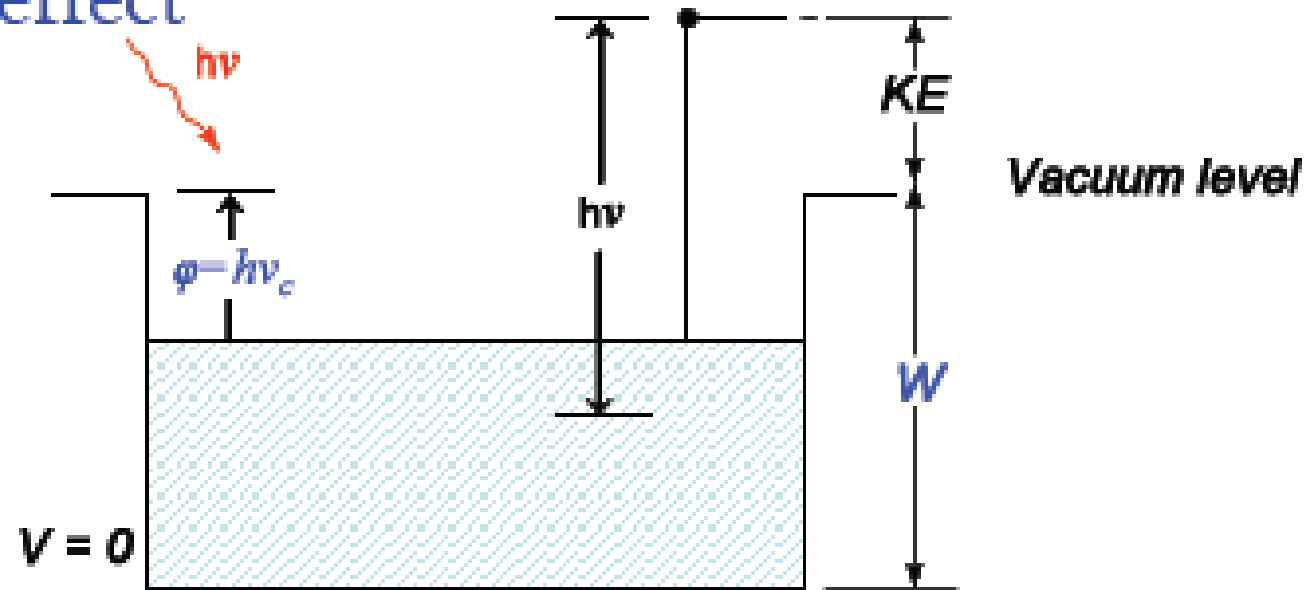


## Diffuse reflectance

- rough surfaces
- at all angles
- $I_{\theta} = I_0 \cos \theta$



# Photoelectric effect

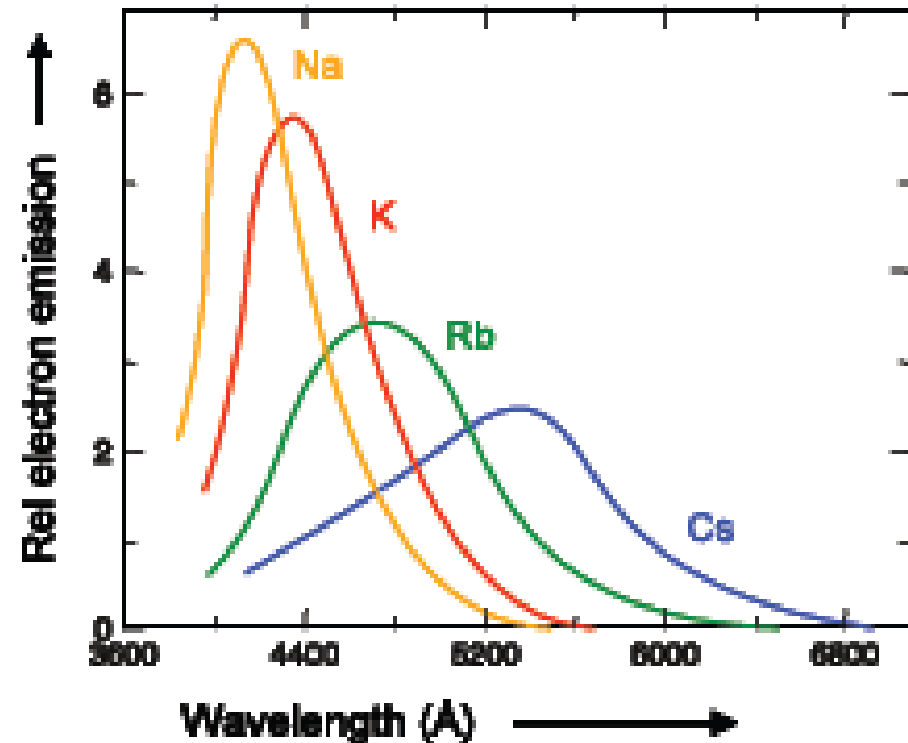


Release of electrons due to absorption of light energy

- potential energy barrier for surface electrons is finite
- critical energy for release:  $\varphi = W - E_f = h \nu_c$
- below  $\nu_c$ : no ejection of photoelectrons
- $\varphi$  characteristic measure

# Photoelectric effect

$$\phi = h \nu_c = \frac{h c}{\lambda_c}$$

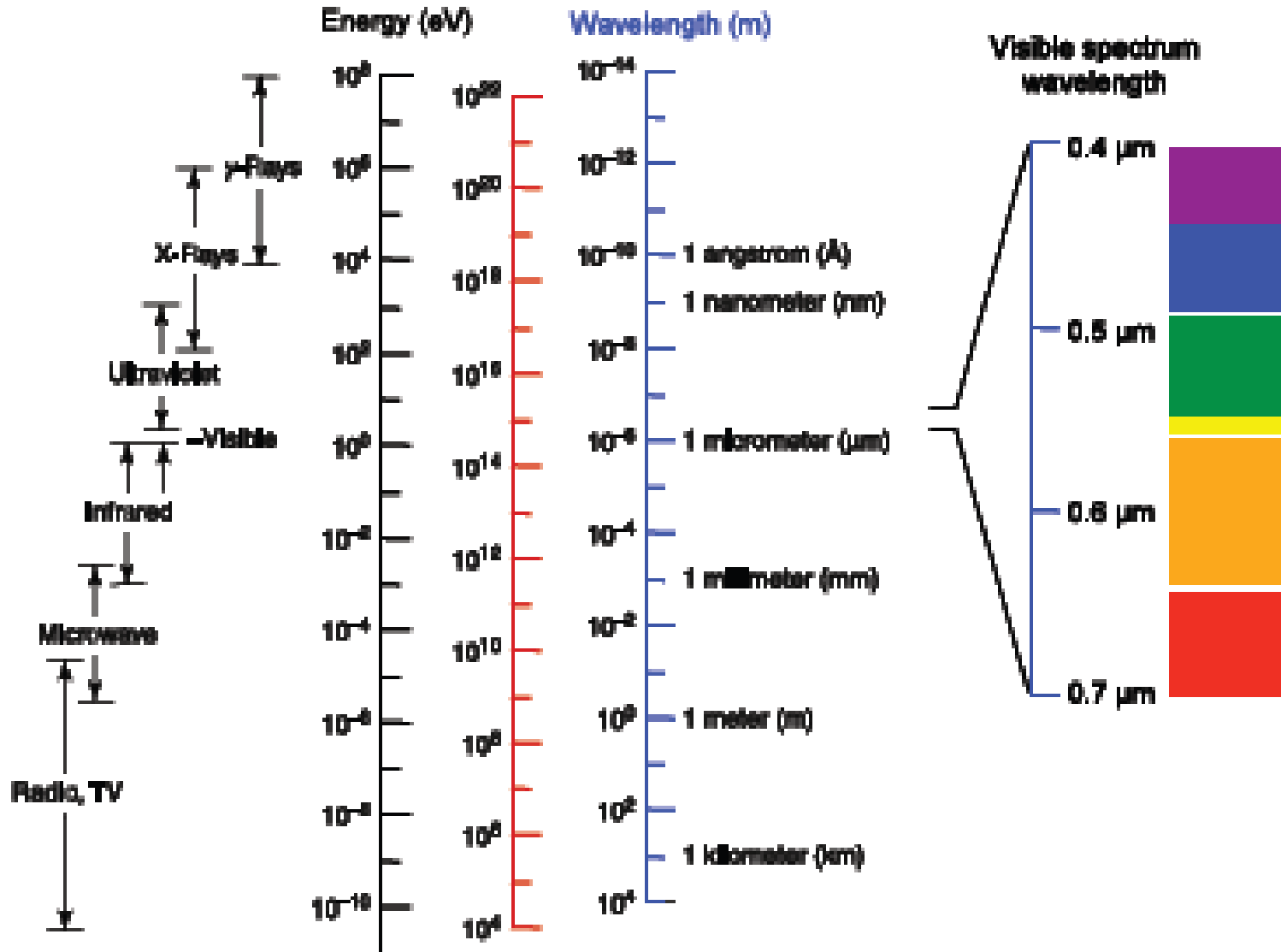


## Photoelectric emission depending on wavelength

- optimal emission at  $\lambda_c$
- below  $\lambda_c$ : insufficient energy
- above  $\lambda_c$ : decrease of electronic excitations efficiency

# Electromagnetic spectrum

Frequency (Hz)





# Optical Properties of ceramics and glasses

## Refractive index $n$

- velocity of light in vacuum:  $c = 299\,792\,458$  m/s
- velocity of light in any other medium:  $v$  ( $v < c$ )
- refractive index  $n = c/v$

- $c$  can be related to  $\epsilon_0$  and  $\mu_0$
- $v$  can be related to  $\epsilon$  and  $\mu$

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$

$$v = \frac{1}{\sqrt{\epsilon \mu}}$$

$$n = \sqrt{\frac{\epsilon_r}{(1 + \chi)}}$$

- ceramics possess small susceptibilities:

$$n \approx \sqrt{\epsilon_r}$$

## Refractive index

Values between  $\approx 1$  and  $\approx 4$

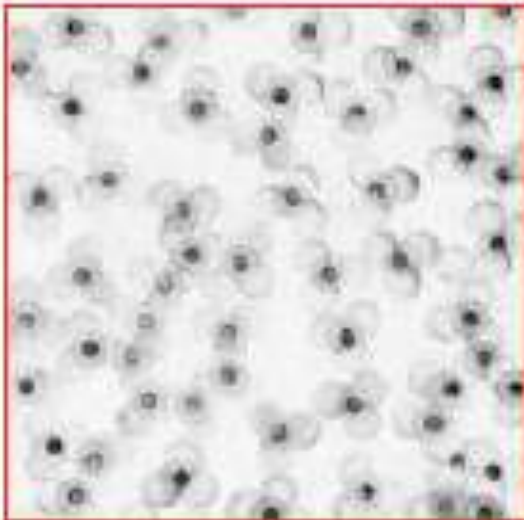
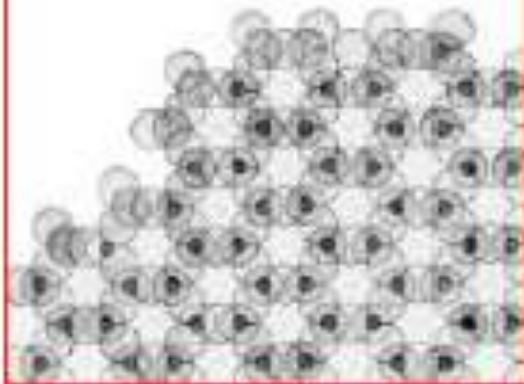
- air: 1.003
- silicate glasses: 1.5 to 1.9
- solid oxide ceramics:  $\approx 2.7$

Dependent on structure-type and packing geometry

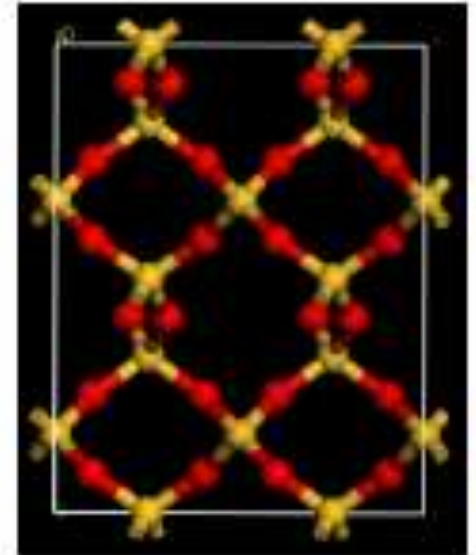
- glasses and cubic crystals:  $n$  is independent of direction
- other crystal systems:  $n$  larger in closed-packed directions
- $\text{SiO}_2$ : glass = 1.46, tridymite = 1.47, cristobalite = 1.49  
quartz = 1.55

## Cristalline silicate *vs* glass

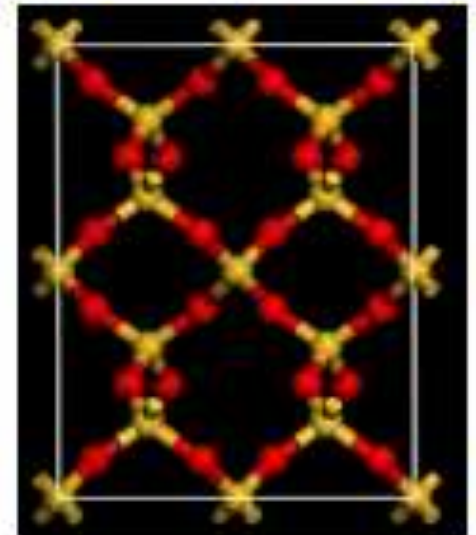
TEM images



Quartz



Addition of large ions  
(Pb, Ba) to  
SiO<sub>2</sub> structures  
increases  $n$  significantly



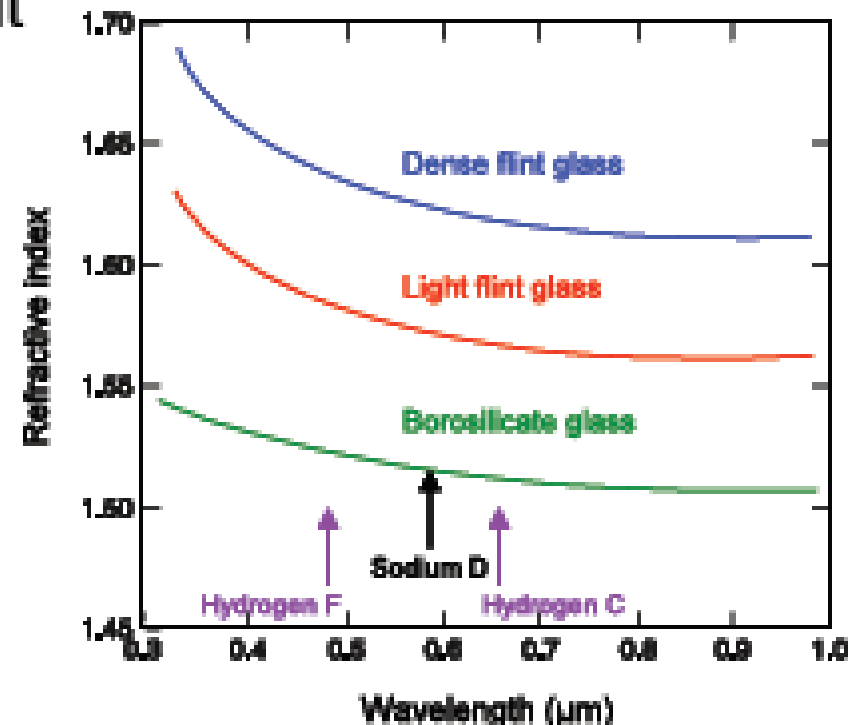
## Refractive index

Mechanical distortions of isotropic glasses changes  $n$

- tensile stress: lower  $n$  normal to direction of applied stress
- compression: higher  $n$  normal to direction of applied stress

$n$  dependent on frequency of light

$$Dispersion = \frac{dn}{d\lambda}$$



## Reflection and refraction

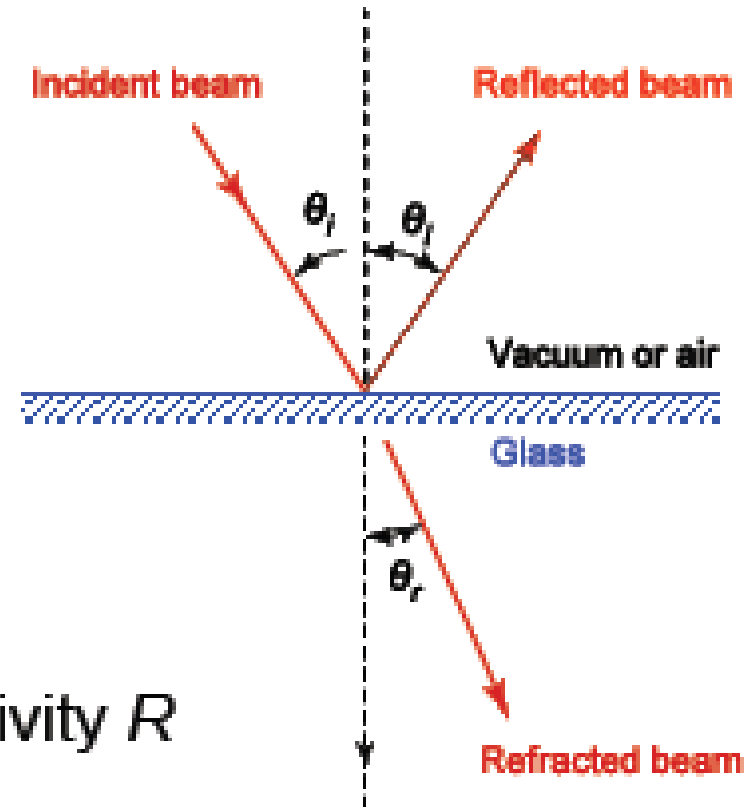
$n$  can be expressed with the angles of incidence and refraction

$$n = \frac{\sin \theta_i}{\sin \theta_r}$$

$n$  can be used to describe reflectivity  $R$

$$R = \frac{I_R}{I_0} = \frac{(n - 1)^2}{(n + 1)^2}$$

$n$  and  $R$  vary with wavelength



## Absorbance and color

Non-reflected light can be transmitted or absorbed

Absorption process is a function of energy (wavelength)

Absorption: fractional change of light intensity  $\frac{dI}{dx} = -\beta dx$

Absorption coefficient  $\beta$  is a material property and a function of the wavelength  $\beta = \frac{4\pi k}{\lambda}$

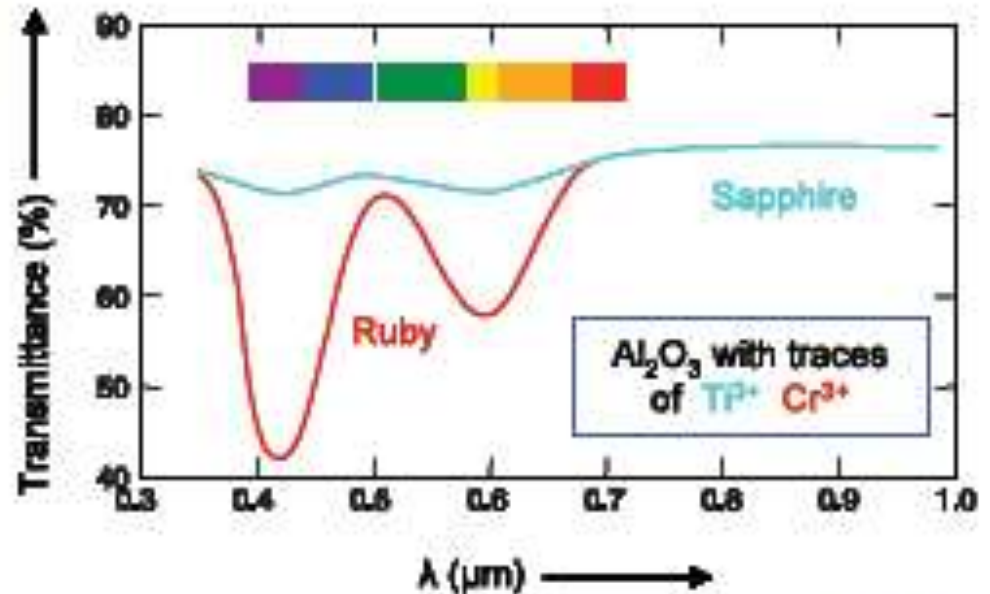
Absorption of photon: excitation of electron from valence to conduction band. Only if photon energy  $>$  band gap  $h\nu \geq E_g$

Magnitude of band gap determines if the material

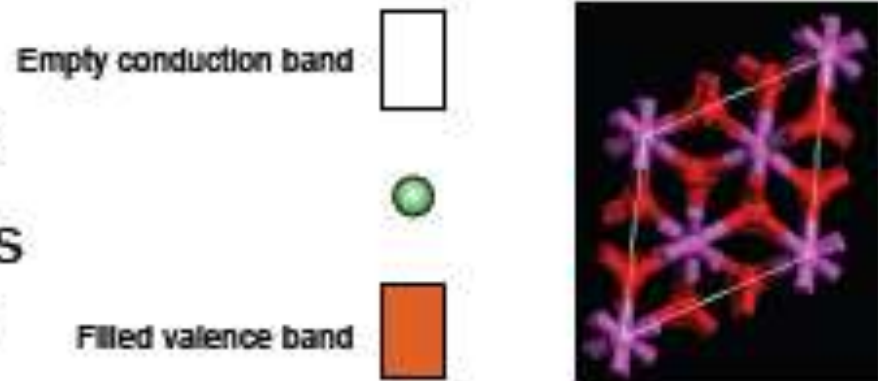
- does not absorb (transparent)
- absorbs certain wavelength (opaque)

# Absorbance and color

Absorption of certain wavelength results in color



Generating color in ceramics:  
 Addition of transition elements  
 with incomplete d band filling  
 V, Cr, Mn, Fe, Co, Ni



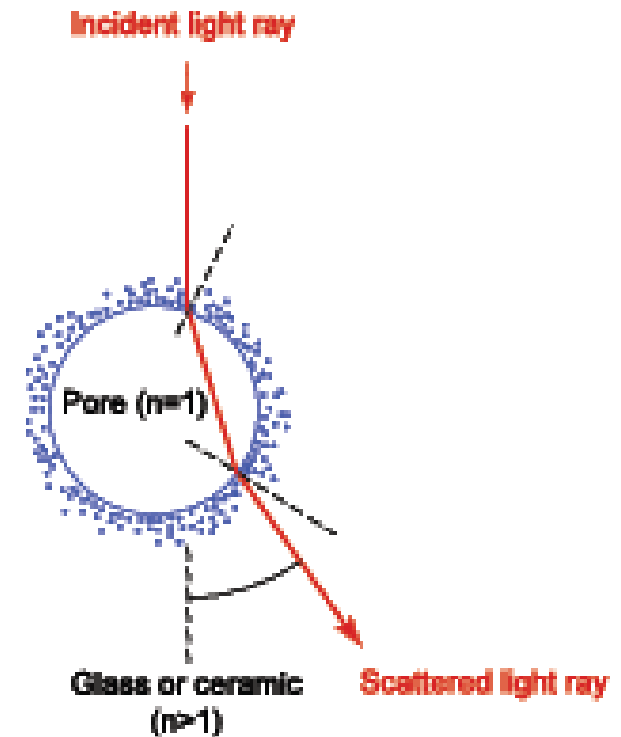
Ruby: Corundum structure  
 with point defects of  $\text{Cr}^{3+}$

# Light scattering in solids

Some inherently transparent materials appear “milky”: translucency

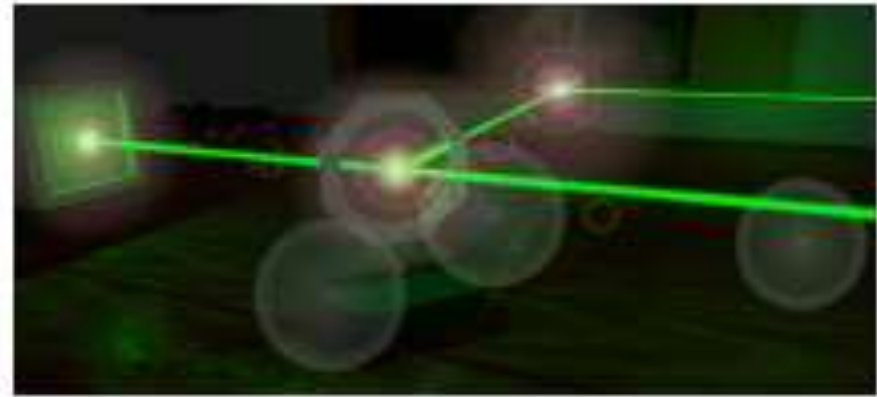
## Scattering

- Pores ( $n_{\text{pore}} < n_{\text{solid}}$ )
- second-phase particles ( $\text{SnO}_2$ ) ( $n_{\text{2nd phase}} > n_{\text{solid}}$ )





# Optical devices



Examples: laser, photodiodes, optical fiber, light emitting diodes

## Semiconductor lasers

Increasingly important in

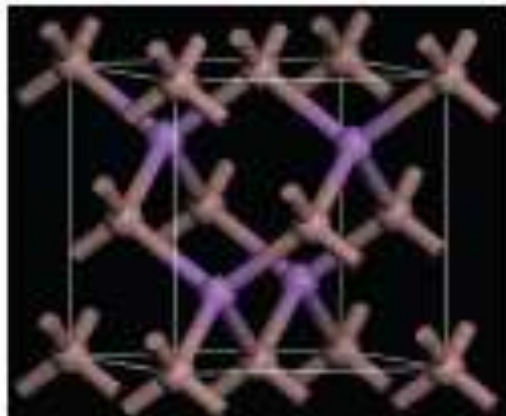
- information storage (CD, DVD)

Layered semiconductor

- applied voltage excites electrons into conduction band
- recombination of electron-hole pair leads to emission

III-V semiconductors

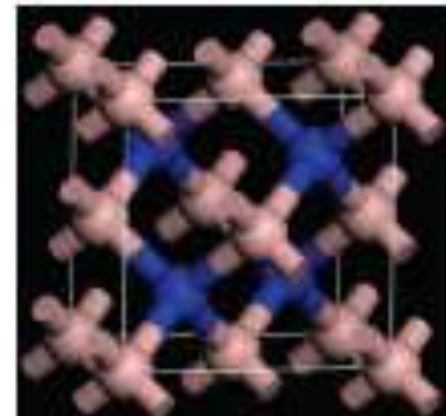
- GaAs (IR, red)



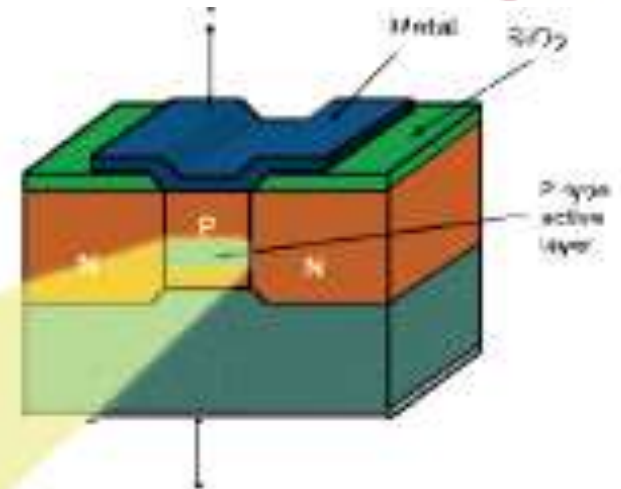
CD

nitrides

- (B,Al,Ga,In)N (blue)



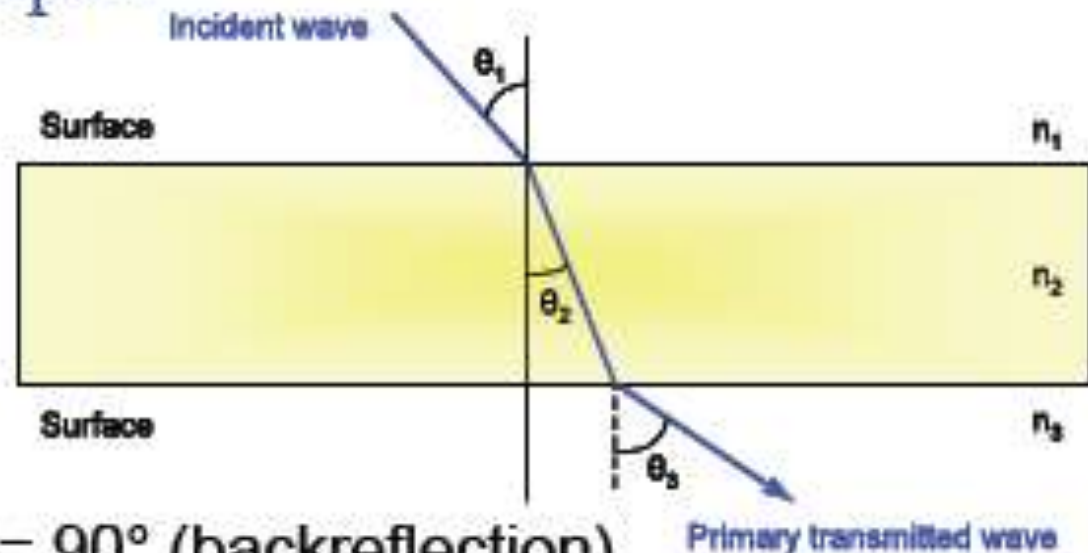
DVD



# Optical fibers - principles

## Total internal reflection

$$\frac{n_2}{n_1} = \frac{\sin \theta_1}{\sin \theta_2} \quad \frac{n_3}{n_2} = \frac{\sin \theta_2}{\sin \theta_3}$$



At some angles of  $\theta_2$ :  $\theta_3 = 90^\circ$  (backreflection)

*Critical angle for total internal reflectance  $\theta_c$*

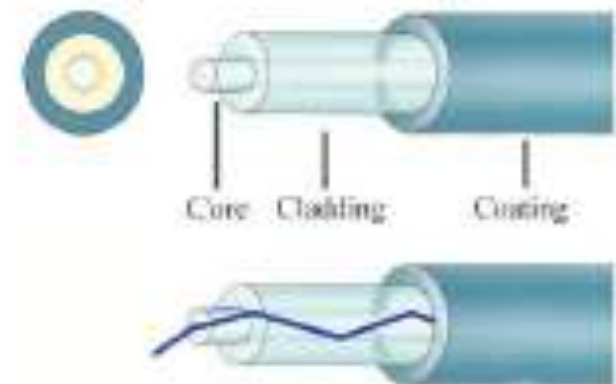
Example: Medium 1 and 3: air, Medium 2: glass with  $n_2 = 1.5$

•  $\theta_3 = 90^\circ$  if  $\theta_c = 42^\circ$

Optical fibers:

Medium 3: glass with  $n_3 < n_2$

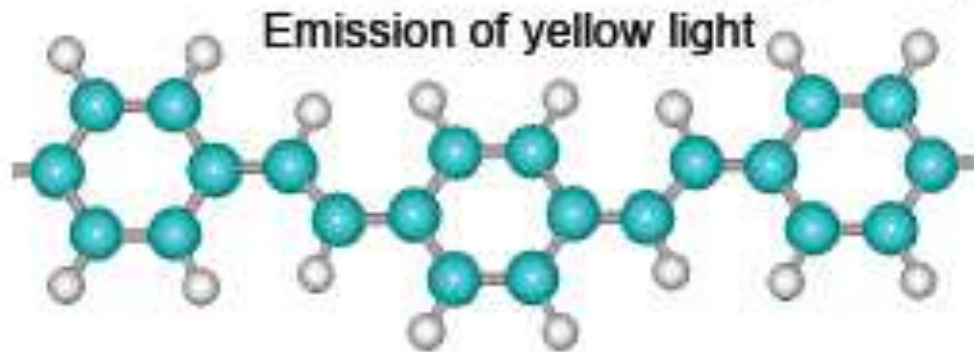
Core and cladding structure



# Electroluminescence

applied voltage excites electrons into conduction band  
 recombination of electron-hole pair leads to emission

First visible light emitting polymer: poly(p-phenylene vinylene)



Polythiophene

Emission of blue light

