

Fracture Mechanics

- It was shown that the theoretical cohesive stress is much greater than the observed fracture stress for metals
- This lead to the idea of defects or cracks which locally raise the stress to the level of the theoretical cohesive stress.
- The first successful theoretical approach for brittle fracture was introduced by Griffith.
- Griffith's equation shows a strong dependence of fracture strength on crack length.
- It is well established that even metals which fail in a completely brittle manner have undergone some plastic deformation prior to fracture.
- Therefore Griffith's theory was modified by Orowan to allow for the degree of plasticity always present in the brittle fracture of metals by the inclusion of a term γ_p which referred to plastic work required to extend the crack wall.





• Orowan;

$$\sigma_f = \left(\frac{2E(\gamma_s + \gamma_p)}{\pi a}\right)^{1/2} \approx \left(\frac{E\gamma_p}{a}\right)^{1/2} \qquad 2.2 - 1$$

where, *E* is Young's modulus and γ_p is the plastic work required to extend the crack wall for a crack of length 2a.

(note: The surface energy term can be neglected since estimates of the plastic work term are about 10^2 to 10^3 J/m² compared with values of γ_s of about 1 to 2 J/m².





Eq 2.2-1 was modified by *Irwin* to replace the hard to measure γ_p with a term that was directly measurable.

$$\sigma_{f}$$
 = {(E $\boldsymbol{\mathscr{G}}_{c}$)/ (π a) }^{1/2}

 \mathcal{G}_{c} corresponds to a critical value of crack-extension force and represent $2\gamma_{p}$.

- The critical value of *G* makes the crack propagate to fracture is called the toughness of the material.



MODE OF FRACTURE

There are three modes of fracture: Mode I, II and III.

Mode I.

Also known as the opening mode, which refers to the applied tensile loading. The most common fracture mode and used in the fracture toughness testing. And a critical value of stress intensity determined for this mode would be designated as K_{IC} .

Mode II.

Also known as the shear mode, which refers to the applied shear stress in the in-plane direction. The shear stress applied normal to the leading edge of the crack but in the plane of the crack.

Mode III.

Also known as the tearing mode, which refers to the applied shear stress out of plane. Applied shear stress is parallel to the leading edge of the crack.

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LINEAR ELASTIC FRACTURE MECHANICS (LEFM)

- Fracture mechanics is the discipline that allows one to assess the importance of cracks in components, irrespective of the mechanism by which the cracks grow.
- LEFM analysis is based on an analytical procedure that relates <u>the stress-field</u> magnitude and distribution in the vicinity of a crack tip to the nominal <u>stress</u> <u>applied</u> of the structural component, to the <u>size</u>, <u>shape and orientation of the crack</u> and to <u>material properties</u>.
- The fundamental principle of fracture mechanics is that the stress field ahead of a sharp crack in a structural member can be characterized in terms of a simple parameter K, the stress intensity factor (was developed by Irwin in the 1950's). This parameter, K, is related to both the nominal stress level (σ) and the size of the crack present (a).



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LINEAR ELASTIC FRACTURE MECHANICS (LEFM)

Fracture <u>The crack tip stresses</u> can be expressed as:

 $\sigma_{ij} = \frac{K_I}{\sqrt{2\pi r}} f_{ij}(\theta)$

Where σ_{ij} are the stresses acting on a material element dxdy at a distance r from the crack tip and at an angle θ from the crack plane, and f_{ij} (θ) are known functions of θ. KI is the stress intensity factor.



Stresses at a point ahead of the crack tip





LINEAR ELASTIC FRACTURE MECHANICS (LEFM)

From the stress field solution it appears that the stresses on a material element as shown in Figure can be described by:

$$\sigma_x = \frac{K_I}{\sqrt{2\pi r}} \cos\frac{\theta}{2} (1 - \sin\frac{\theta}{2}\sin\frac{3\theta}{2})$$

$$\sigma_y = \frac{K_I}{\sqrt{2\pi r}} \cos\frac{\theta}{2} (1 + \sin\frac{\theta}{2}\sin\frac{3\theta}{2})$$

$$\sigma_z = 0$$

$$\tau_{xy} = \frac{K_I}{\sqrt{2\pi r}} \cos\frac{\theta}{2} \sin\frac{\theta}{2} \cos\frac{3\theta}{2}$$

For an orientation directly ahead of the crack, $\theta = 0$, then $\tau_{xy} = 0$ and x = r.



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• The crack tip stress must be proportional to the applied stress σ .



The crack tip stresses will also depend upon crack size. The stresses will be higher when "a" is longer. Hence the crack size "a" must appear in the numerator in equation





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The crack tip stress must be proportional to the applied stress σ .



• With $C = (\pi)^{1/2}$, then

We get:



Comparing the above equation with





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- K depends on the plate dimensions, for example width W
- As W decreases, the stress at the crack tip increases
- For any configuration the crack tip stresses will be:



Dividing C/ (π)^{1/2} and substitute \sqrt{a} with $\sqrt{\pi a}$

 $C(a/L)/(\pi)^{1/2} = \beta.$

$$\sigma_{y} = \frac{\beta \sigma \sqrt{\pi a}}{\sqrt{2\pi x}} = \frac{K_{I}}{\sqrt{2\pi x}}$$

The stress intensity factor is always:



(note: β is a dimensionless parameter or function that depends on both crack and specimen sizes and geometries, as well as the manner or load application and also can be written as Y or α).

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- For an infinite plate, $\beta = 1$
- (for planar specimens containing cracks that are much shorter than the specimen width)
- e.g. for a plate of infinite width having a throughthickness crack.

 $K_I = \beta \sigma \sqrt{\pi a} = \sigma \sqrt{\pi a}$

- For a semi-infinite plate, $\beta = 1.12$ and
- (for a plate of semi-infinite containing an edge crack of length a)



For a circular (penny-shaped) crack with radius (α), $\beta = 2/\pi$ and





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DESIGN USING FRACTURE MECHANIC (TOUGHNESS)

- A property that is a measure of a material's resistance to brittle fracture when a crack is present.
- From an engineering point of view, the stress intensity factor K_I can be used as stress to predict the *critical condition at fracture*

Fracture occurs when:







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GEOMETRY, LOAD, & MATERIAL

K ≥Kc

Condition for crack propagation:

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Stress Intensity Factor: --Depends on load & geometry.

Fracture Toughness: --Depends on the material, temperature, environment, & rate of loading.

• Values of K for some standard loads & geometries:





Relation between fracture toughness and allowable stress and crack size



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DESIGN EX: AIRCRAFT WING

- Material has $K_c = 26 \text{ MPa-m}^{0.5}$
- Two designs to consider...

Design A --largest flaw is 9 mm --failure stress = 112 MPa

• Use...
$$\sigma_c = \frac{K_c}{Y_v \pi a_{max}}$$

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• Key point: Y and K_c are the same in both designs.

• Reducing flaw size pays off!
--Result:
4 mm

$$\left(\sigma_{c}\sqrt{a_{max}}\right)_{A} = \left(\sigma_{c}\sqrt{a_{max}}\right)_{B}$$

Answer: $\left(\sigma_{c}\right)_{B} = 168 MPa$
 $\left(\sigma_{c}\right)_{B} = 168 MPa$



Loading Rate

Increased loading rate...
 -- increases σ_y and TS
 -- decreases %EL

• why? An increased rate gives less time for dislocations to move past obstacles.





MEASUREMENT OF FRACTURE TOUGHNESS

- Fracture toughness is a material property which characterise the crack resistance and the value of K_{IC} can be found by testing of the same material with different geometries and with combinations of crack size and fracture stress.
- Knowledge of K_{IC} under standard conditions can be used to predict failure







Kı

MEASUREMENT OF FRACTURE TOUGHNESS

K_{IC} is usually measured under plane strain conditions, and the minimum thickness, B of the test specimen to achieve plane strain is:

 $B \ge 2 \cdot 5$



THICKNESS

Effect of specimen thickness on K_{IC}



 σ_{vs} is the 0.2 % offset yield strength

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FRACTURE TOUGHNESS: Specimen Configurations

- Several types of specimens are permitted in ASTM standards
- Compact tension (CT) specimens and single edge notched bend (SENB) are the most common.





K_{IC} Testing

- First, cyclic loading (Fatigue) is applied to introduce a crack.
 When this crack is at the desired length the cycling is stopped and the load is raised until fracture occurs.
- The stress intensity at fracture can then be calculated; (i. e: K_{IC}).

$$K_Q = \frac{P_5}{BW^{1/2}} f\left(\frac{a}{W}\right)$$
 (Candidate value)

Check for B>2.5 $(K_Q/\sigma_{ys})^2$. If OK, then $K_{IC} = K_Q$. If not a <u>new test</u> <u>must be done on a thicker</u> <u>specimen.</u>





Type I

Load-displacement curve represents the behavior for a wide variety of ductile metals. The crack propagates by tearing mode with increasing load.

Type II

Load displacement curve has a point where there is a sharp drop in load followed by a recovery load. The load drop arises from sudden unstable, rapid crack propagation before the crack slows-down to a tearing mode of propagation.

Type III

Instability. Initial crack movements propagates rapidly to complete failure. Characteristic of a very brittle "elastic material'.



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Impact testing

- Standard laboratory tensile test could not extrapolated to predict fracture behavior e.g. under some circumstances ductile metal can fracture abruptly and with very little plastic deformation.
- Type of materials to be tested: which have
 - 1. Deformation at a relatively low temperature
 - 2. A high strain rate (e.g. rate of deformation)
 - 3. A triaxial stress state (which may be introduced by the presence of a notch.



Impact Testing

- Impact loading:
- -- severe testing case
 -- makes material more brittle
 -- decreases toughness



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Charpy-Izod Impact test

one of the primary function : to determine whether or not a material experiences a ductile-to-brittle transition.

ductile-to-brittle transition

Is related to the temperature dependence of the measured impact energy absorption.

- At higher temperatures the charpy v-notch (CVN) is relatively large (refer to ductile mode of fracture)
- Low temperature: the impact energy drops suddenly over a relatively narrow temperature range (small energy , brittle fracture)





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Temperature

• Increasing temperature...

--increases %EL and Kc

Ductile-to-Brittle Transition Temperature (DBTT)...





- For material that exhibit ductile-brittle behavior should be used only above this transition temperature, to avoid brittle and catastrophic failure.
 - Example: Titanic and Liberty ship
 - Vessel material : steel alloy which has adequate ductility at room temperature tensile test.
 - accident occurred at ~ 4°C
 - Each fracture crack originated at some point of stress concentration e.g. at sharp corner or fabrication defect, then propagated around the entire girth of the ship





Materials which experienced a ductile-to-brittle transition

 Low strength steel , BCC crystal structure
 The transition temperature is sensitive to both alloy composition and microstructure.

e.g.

- decreasing the average grain size results in a lowering of the transition temperature (strengthen and toughen the steels)
- Increasing the carbon content: strength increase, raises the CVN transition temperature



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Materials which do not experienced a ductile-to-brittle transition

- Low strength FCC metals (some Al and Cu alloys) and most HCP metals, and always retain high impact energies or remain ductile with decreasing temperature.
- High strength materials e.g. high strength steel and titanium alloys. Impact energy is relatively insensitive to temperature but these materials are very brittle, reflected by their low impact energy values.







TYPES OF FRACTURE

- In general, materials can be broadly classified into two groups depending on their mechanical behaviour.
 - 1. Materials that behave in a **ductile** manner
 - 2. materials that behave in a **brittle** (cleavage) manner.

Ductile fracture is high energy fracture and occurs with large plastic deformation. Characterised by stable crack growth

> Brittle fracture is low energy fracture and occurs with no or little plastic deformation. Characterised by unstable crack growth



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MECHANISM OF DUCTILE FRACTURE

The observed stages in ductile fracture are as follows:

- 1. Formation of voids around an inclusion or second phase particles
- 2. Growth of the void around the particles
- 3. Coalescence of the growing void with adjacent voids.





SUMMARY

- Engineering materials don't reach theoretical strength.
- Flaws produce stress concentrations that cause premature failure.
- Sharp corners produce large stress concentrations and premature failure.





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